Temporal ontologies

Modelling with temporal ontologies Summary

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# COMP718: Ontologies and Knowledge Bases Lecture 11: Temporal Ontologies

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Temporal ontologies

Modelling with temporal ontologies Summary

### Outline

#### Introduction: why temporal ontologies?

- Introduction
- Temporal operators and relations

#### 2 Temporal ontologies

- Time ontology
- DLR<sub>US</sub>

#### 3 Modelling with temporal ontologies

- Essential and immutable parts (details in [AGK08])
- Transforming objects (details in [Kee09])

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Temporal ontologies

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Introduction

# Which kind of temporal things?

#### Actual dates, time, intervals

- Qualitative temporal relations, such as: before, after, during, while, meet (Allen temporal relations), precedes and immediately precedes (recollect OBO foundry relations)
- More advanced relations; e.g., *transformation\_of*, *developed\_from*, *derived\_from*
- Temporalising classes (cf. 'object migration' in databases); e.g., an <u>active</u> project evolves to completed project
- Temporalising relations; e.g. 'during the <u>lifetime</u> of x, it always has y as part', 'every passenger that boards the plane must <u>have</u> check<u>ed</u> in between 24h and 0.5h <u>before</u> the <u>scheduled</u> departure of that flight' [KA10]

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## Examples

- Buttery is a transformation of Caterpillar, using both LTL and the phased sortals of OntoClean [Kee09]
- Brain is specific dependent part of Human body, using temporalisation of the parthood relation [AGK08]
- Bypass sometimes comes after the grafting [SSBS09] in SNOMED CT, using CTL then we have E[grafting U bypass]
  - Note shorthand CTL notations: E: exists a path; A: in all paths; F: some time in the future; G: globally in the future; X: next time; and U for p until q
- Brain concussion with loss of consciousness [SSBS09] in SNOMED CT

Summarv

Temporal ontologies

Modelling with temporal ontologies Summary

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#### Introduction

- The usual ones (satisfiability, subsumption, etc.)
- Querying temporal knowledge bases
  - "In which year in the previous century was the great flooding disaster (watersnoodramp) in the Netherlands?"
  - "Who was the South African president before Jacob Zuma?"
- Logical implications; e.g. given  $B \sqsubseteq A$ , then
  - objects active in B must be active in A (e.g., if one is a student (B) then one is also a person (A)),
  - objects scheduled to become active in B must exist in A (e.g., an employee (A) is up for promotion to become a manager (B))
- A range of other examples, a.o.:
  - Reasoning with a calendar hierarchy and across calendars
  - Finding a solution satisfying a set of constraints for scheduling the lecture hours of a study programme.

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Temporal ontologies

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Introduction

## Many issues to investigate

- Temporal logic and modelling issues in ontology development
- Interaction temporal logic and temporal databases
- Temporal logic and verification (formal methods)
- Interaction (temporal) DLs with (temporal) conceptual data modelling
- Computational properties of various fragments of expressive temporal logics
- Linear vs. branching time and endurantism vs. perdurantism in philosophy

Temporal ontologies

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Temporal operators and relations

## Principal models of time





Figure: Top: linear, with corresponding LTLs; Bottom: branching time, with corresponding CTLs to formalise it.

Temporal ontologies

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Temporal operators and relations

## Temporal operators in LTL

- until,  $\phi$  **U**  $\psi$ ,  $\phi$   $\mathcal{U}$   $\psi$ ,  $\phi$  holds until  $\psi$
- since,  $\phi$  **S**  $\psi$ ,  $\phi$   $\mathcal{S}$   $\psi$ ,  $\phi$  holds since  $\psi$
- next,  $\mathbf{N}\phi$ ,  $\bigcirc\phi$ :  $\phi$  has to hold at the next state
- future,  $\mathbf{F}\phi$ ,  $\Diamond\phi$ :  $\phi$  must hold eventually
- globally  $\mathbf{G}\phi$ :  $\Box\phi$  must hold always (entire subsequent path)
- More precise, e.g.: must have held some time in the past  $\Diamond^- \phi,$  etc.

Temporal ontologies

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Temporal operators and relations

## Intuition of the operators in CTL

finally P



AF p



globally P

AGP



next p

AX p





A[pUq]



EF P



EXp



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Temporal operators and relations

## Allen temporal relations<sup>1</sup>

Relation	Symbol	Symbol for Inverse	Pictoral Example
X before Y	<	>	ХХХ ҮҮҮ
X equal Y	=	=	XXX YYY
X meets Y	m	mi	XXXYYY
X overlaps Y	0	oi	XXX YYY
X during Y	d	di	XXX YYYYYY
X starts Y	s	si	XXX YYYYY
X finishes Y	f	fi	XXX YYYYY

#### FIGURE 2. The Thirteen Possible Relationships.

<sup>1</sup>James F. Allen. Maintaining knowledge about temporal intervals. *Communications of the ACM*, 26(11), 1983.

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Introduction:	why	temporal	ontologies?

Temporal ontologies

#### Time ontology

#### Overview

- An ontology to describe the temporal content of Web pages and the temporal properties of Web services
- Vocabulary for expressing facts about topological relations among instants and intervals, together with information about durations, and about datetime information
- OWL encoding and a first-order logic axiomatization of the ontology
- It is an ontology to *talk* about time, but **not** to *represent and reason over* temporal knowledge, i.e., a 'workaround'

more info at http://www.w3.org/TR/owl-time/

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Time ontology

## Core: Topological Temporal Relations

- TemporalEntity with two subclasses Instant and Interval
- hasBeginning and hasEnd are relations between instants and temporal entities
- inside is a relation between an instant and an interval
- before relation on temporal entities, which gives directionality to time, but is not enforced in the language
- Interval relations, such as intervalEquals, intervalBefore, intervalMeets etc.

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Time ontology

# Core: Duration Description

- An interval can have multiple duration descriptions (e.g., 2 days, 48 hours), but can only have one duration
- Different sets of properties for DateTimeDescription and DurationDescription, because their ranges are different.
  - year (in DateTimeDescription) has a range of xsd:gYear, while years (in DurationDescription) has a range ofxsd:decimal so that you can say duration of 2.5 years.
- durationOf that takes eight arguments, but split up into 8 binaries
- Other components: Time Zones, DateTime Description

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#### $DLR_{US}$

# Syntax of $\mathcal{DLR}_{\mathcal{US}}$

- DLR<sub>US</sub> [AFWZ02] combines the PTL with Since and Until and the DL DLR [CDG03], i.e., a expressive fragment of L{since, until}
  - Classes, *n*-ary relations ( $n \ge 2$ ), role components
  - Binary constructors (⊓, ⊔, U, S) for relations of the same arity, and all boolean constructors for both class and relation expressions
- For both classes and relations: temporal operators  $\Diamond^+$ ,  $\oplus$ , and their past counterparts can be defined via  $\mathcal{U}$  and  $\mathcal{S}$ :  $\Diamond^+ C \equiv \top \mathcal{U} C$ ,  $\Diamond^- C \equiv \top \mathcal{S} C$ ,  $\oplus C \equiv \bot \mathcal{U} C$ , etc;  $\Box^+$  and  $\Box^-$  as  $\Box^+ C \equiv \neg \Diamond^+ \neg C$ and  $\Box^- C \equiv \neg \Diamond^- \neg C$ .  $\Diamond^*$  and  $\Box^*$  as  $\Diamond^* C \equiv C \sqcup \Diamond^+ C \sqcup \Diamond^- C$  and  $\Box^* C \equiv C \sqcap \Box^+ C \sqcap \Box^- C$ .
  - $C \rightarrow \top | \perp | CN | \neg C | C_1 \sqcap C_2 | C_1 \sqcup C_2 | \exists^{\leq k} [U_j]R |$  $\Diamond^+ C | \Diamond^- C | \Box^+ C | \Box^- C | \oplus C | \ominus C | C_1 \mathcal{U} C_2 | C_1 \mathcal{S} C_2$
- $\begin{array}{rcl} R & \rightarrow & \top_n & \mid RN \mid \neg R \mid R_1 \sqcap R_2 \mid R_1 \sqcup R_2 \mid U_i/n : C \mid \\ & & \Diamond^+ R \mid \Diamond^- R \mid \Box^+ R \mid \Box^- R \mid \bigoplus R \mid \bigoplus R \mid B_1 \upharpoonright \mathcal{U} R_2 \vDash R_1 \mathrel{\overset{\circ}{\otimes}} R_2 \overset{\simeq}{=} \begin{array}{c} & & \bigcirc \land \land \\ & & 16/66 \end{array}$

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 $DLR_{US}$ 

## Semantics of $\mathcal{DLR}_{\mathcal{US}}$

Interpreted in *temporal models* over *T* (where *T* = ⟨*T<sub>p</sub>*, <⟩), which are triples of the form *I* ≐ ⟨*T*, Δ, .<sup>*I*(t)</sup>⟩, where Δ is the *domain* of *I* and .<sup>*I*(t)</sup> an *interpretation function* s.t., for every *t* ∈ *T*, every *C*, and *R*, we have *C<sup>I(t)</sup>* ⊆ Δ and *R<sup>I(t)</sup>* ⊆ (Δ)<sup>n</sup>.
note: (*u*, *v*) = {*w* ∈ *T* | *u* < *w* < *v*}.

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 $DLR_{US}$ 

## Semantics of $\mathcal{DLR}_{US}$

$$\begin{split} \top^{\mathcal{I}(t)} &= \Delta^{\mathcal{I}}; \ \perp^{\mathcal{I}(t)} = \emptyset; \ CN^{\mathcal{I}(t)} \subseteq \top^{\mathcal{I}(t)}; \ (\neg C)^{\mathcal{I}(t)} = \top^{\mathcal{I}(t)} \setminus C^{\mathcal{I}(t)}; \\ (C_1 \sqcap C_2)^{\mathcal{I}(t)} &= C_1^{\mathcal{I}(t)} \cup C_2^{\mathcal{I}(t)}; \\ (G_1 \sqcup C_2)^{\mathcal{I}(t)} &= C_1^{\mathcal{I}(t)} \cup C_2^{\mathcal{I}(t)}; \\ (\exists^{\leq k}[U_j]R)^{\mathcal{I}(t)} &= \{ \ d \in \top^{\mathcal{I}(t)} \mid \exists \{ \langle d_1, \dots, d_n \rangle \in R^{\mathcal{I}(t)} \mid d_j = d \} \leq k \}; \\ (C_1 \sqcup C_2)^{\mathcal{I}(t)} &= \{ \ d \in \top^{\mathcal{I}(t)} \mid \exists v > t.(d \in C_2^{\mathcal{I}(v)} \land \forall w \in (t, v).d \in C_1^{\mathcal{I}(w)}) \}; \\ (C_1 S C_2)^{\mathcal{I}(t)} &= \{ \ d \in \top^{\mathcal{I}(t)} \mid \exists v < t.(d \in C_2^{\mathcal{I}(v)} \land \forall w \in (v, t).d \in C_1^{\mathcal{I}(w)}) \}; \\ (T_n)^{\mathcal{I}(t)} \subseteq (\Delta^{\mathcal{I}})^n; \ RN^{\mathcal{I}(t)} \subseteq (\top_n)^{\mathcal{I}(t)}; \ (\neg R)^{\mathcal{I}(t)} = (\top_n)^{\mathcal{I}(t)} \setminus R^{\mathcal{I}(t)}; \\ (R_1 \sqcap R_2)^{\mathcal{I}(t)} &= R_1^{\mathcal{I}(t)} \cup R_2^{\mathcal{I}(t)}; \\ (R_1 \sqcup R_2)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \exists v > t.(\langle d_1, \dots, d_n \rangle \in R_2^{\mathcal{I}(v)} \land \forall w \in (v, v). \langle d_1, \dots, d_n \rangle \in R_1^{\mathcal{I}(w)}) \}; \\ (R_1 S R_2)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \exists v > t.(\langle d_1, \dots, d_n \rangle \in R_2^{\mathcal{I}(v)} \land \forall w \in (v, t). \langle d_1, \dots, d_n \rangle \in R_1^{\mathcal{I}(w)}) \}; \\ (\Diamond^{\leftarrow} R)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \exists v > t. \langle d_1, \dots, d_n \rangle \in R^{\mathcal{I}(v)} \}; \\ (\oplus R)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \exists v > t. \langle d_1, \dots, d_n \rangle \in R^{\mathcal{I}(v)} \}; \\ (\ominus R)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \exists v < t. \langle d_1, \dots, d_n \rangle \in R^{\mathcal{I}(v)} \}; \\ (\ominus R)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \exists v < t. \langle d_1, \dots, d_n \rangle \in R^{\mathcal{I}(v)} \}; \\ (\ominus R)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \exists v < t. \langle d_1, \dots, d_n \rangle \in R^{\mathcal{I}(v)} \}; \\ (\ominus R)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \exists v < t. \langle d_1, \dots, d_n \rangle \in R^{\mathcal{I}(v)} \}; \\ (\ominus R)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \langle d_1, \dots, d_n \rangle \in R^{\mathcal{I}(v-1)} \}, \\ (\ominus R)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid d_1, \dots, d_n \rangle \in R^{\mathcal{I}(v-1)} \}; \\ (\ominus R)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \langle d_1, \dots, d_n \rangle \in R^{\mathcal{I}(v-1)} \}, \\ (\Box R)^{\mathcal{I}(t)} &= \{ \langle d_1, \dots, d_n \rangle \in (\top_n)^{\mathcal{I}(t)} \mid \langle d_1, \dots, d_n \rangle \in R^{\mathcal{I}(v-1)}$$

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• Need to represent difference between essential vs mandatory vs immutable parts and wholes



- Brain is an essential part of Human
- Heart is a mandatory part of Human but a heart can be transplanted
- Hand is an immutable part of Boxer but a human can do without hands

• More generally: the life cycle semantics of parts and wholes

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Essential and immutable parts (details in [AGK08])

### Defining participation in the relation

- Two criteria: (i) nature of the dependence relationship between the classes and (ii) strength of the participation
  - 1 Generic Dependence Mandatory Part. The whole must have a part at each instant of its lifetime. Thus, the presence of the part is mandatory, but it can be replaced over time (e.g., the human heart example).
  - 2 Unconditional Specific Dependence Essential Part. The part is mandatory, but it cannot be replaced without destroying the whole (e.g., the human brain example).
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Temporal ontologies

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Essential and immutable parts (details in [AGK08])

### Defining participation in the relation

- Two criteria: (i) nature of the dependence relationship between the classes and (ii) strength of the participation
  - 1 Generic Dependence Mandatory Part. The whole must have a part at each instant of its lifetime. Thus, the presence of the part is mandatory, but it can be replaced over time (e.g., the human heart example).
  - 2 Unconditional Specific Dependence Essential Part. The part is mandatory, but it cannot be replaced without destroying the whole (e.g., the human brain example).
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Temporal ontologies

Modelling with temporal ontologies Summary

Essential and immutable parts (details in [AGK08])

# $\mathcal{ER}_{VT}$ : Temporal EER

- For each  $\mathcal{ER}_{VT}$  conceptual data model, there is an equi-satisfiable  $\mathcal{DLR}_{US}$  knowledge base
- Given the set-theoretic semantics for  $\mathcal{ER}_{VT}$ , modelling notions such as satisfiability, subsumption, and derivation of new constraints have been defined [APS07]
- Textual and a graphical syntax along with a model-theoretic semantics as a temporal extension of the EER semantics [CLN99]
- $\mathcal{ER}_{VT}$  [AFWZ02] supports timestamping for classes, attributes, and relationships
- Status classes [APS07] constrain evolution of an instance's membership in a class along its lifespan

Temporal ontologies

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Essential and immutable parts (details in [AGK08])

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Temporal ontologies

#### Essential and immutable parts (details in [AGK08])

### An example



S, snapshot class:  $C \sqsubseteq \Box^* C$ T: temporary class:  $C \sqsubseteq \Diamond^* \neg C$ 

Temporal ontologies

Modelling with temporal ontologies Summary

Essential and immutable parts (details in [AGK08])

#### Status classes



Temporal ontologies

Essential and immutable parts (details in [AGK08])

### Status relations


Temporal ontologies

Essential and immutable parts (details in [AGK08])

# Status relations

- Scheduled: a relation is scheduled if its instantiation is known but its membership will only become effective some time later. e.g., a new pillar for the Sagrada Familia's interior is scheduled to become part of that church.
- Active: the status of a relation is active if the particular relation fully instantiates the type-level relation and only active classes can participate into an active relation; e.g., the Mont Blanc mountain is part of the Alps mountain range

Temporal ontologies

Essential and immutable parts (details in [AGK08])

# Extending $\mathcal{ER}_{VT}$ with status relations

- **Suspended**: to capture a temporarily inactive relation; e.g., an instance of a CarEngine is removed from the instance of a Car it is part of for purpose of maintenance.
- **Disabled**: to model expired relations that never again can be used; e.g., to represent the donor of an organ who has donated that organ and one wants to keep track of who donated what to whom.

Temporal ontologies

Modelling with temporal ontologies Summary

Essential and immutable parts (details in [AGK08])

(ACT) Active relations involve only active classes.  $\langle o_1, o_2 \rangle \in \mathbb{R}^{\mathcal{I}(t)} \to o_1 \in C_1^{\mathcal{I}(t)} \land o_2 \in C_2^{\mathcal{I}(t)}$  $\mathbf{R} \sqsubseteq \mathbf{U}_1 : \mathbf{C}_1 \sqcap \mathbf{U}_2 : \mathbf{C}_2$ (REXISTS) Existence persists until Disabled.  $\langle o_1, o_2 \rangle \in \text{Exists-R}^{\mathcal{I}(t)} \to \forall t' > t.(\langle o_1, o_2 \rangle \in$ Exists- $\mathbb{R}^{\mathcal{I}(t')} \lor \langle o_1, o_2 \rangle \in \mathsf{Disabled}-\mathbb{R}^{\mathcal{I}(t')}$ ) Exists-R  $\sqsubseteq$   $\Box^+$ (Exists-R  $\sqcup$  Disabled-R) (RDISAB1) Disabled persists.  $\langle o_1, o_2 \rangle \in \texttt{Disabled}\texttt{-R}^{\mathcal{I}(t)} o orall t' > t. \langle o_1, o_2 \rangle \in \texttt{Disabled}\texttt{-R}^{\mathcal{I}(t')}$ Disabled-R  $\Box \Box^+$  Disabled-R (RDISAB2) Disabled was Active in the past.  $\langle o_1, o_2 \rangle \in \texttt{Disabled-R}^{\mathcal{I}(t)} \rightarrow \exists t' < t. \langle o_1, o_2 \rangle \in \texttt{R}^{\mathcal{I}(t')}$ Disabled-R  $\Box \Diamond^- R$ (RSUSP1) Suspended was Active in the past.  $\langle o_1, o_2 \rangle \in \text{Suspended-R}^{\mathcal{I}(t)} \to \exists t' < t. \langle o_1, o_2 \rangle \in \mathbb{R}^{\mathcal{I}(t')}$ Suspended-R  $\Box \Diamond^- R$ 

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(RSUSP2) Suspended involve Active or Suspended Classes.  $\langle o_1, o_2 \rangle \in \text{Suspended-R}^{\mathcal{I}(t)} \rightarrow o_i \in C_i^{\mathcal{I}(t)} \lor o_i \in Suspended-C_i^{\mathcal{I}(t)}, i = 1, 2$ Suspended-R  $\sqsubseteq U_i : (C_i \sqcup \text{Suspended-C}_i), i = 1, 2$ 

- (RSCH1) Scheduled will eventually become Active.  $\langle o_1, o_2 \rangle \in \text{Scheduled-R}^{\mathcal{I}(t)} \rightarrow \exists t' > t. \langle o_1, o_2 \rangle \in \mathbb{R}^{\mathcal{I}(t')}$ Scheduled-R  $\sqsubseteq \Diamond^+ \mathbb{R}$
- (RSCH2) Scheduled can never follow Active.  $\langle o_1, o_2 \rangle \in \mathbb{R}^{\mathcal{I}(t)} \rightarrow \forall t' > t. \langle o_1, o_2 \rangle \notin \text{Scheduled-R}^{\mathcal{I}(t')}$  $\mathbb{R} \sqsubseteq \Box^+ \neg \text{Scheduled-R}$

Temporal ontologies

Essential and immutable parts (details in [AGK08])

# Constraints and logical implications

#### PROPOSITION (Status Relations: Logical Implications)

Given the set of axioms  $\Sigma_{st}$  (REXISTS-RSCH2), an n-ary relation (where  $n \ge 2$ )  $R \sqsubseteq U_1 : C_1 \sqcap \ldots \sqcap U_n : C_n$ , the following logical implications hold:

(RACT) Active will possible evolve into Suspended or  
Disabled.  
$$\Sigma_{st} \models R \sqsubseteq \Box^+(R \sqcup \text{Suspended-}R \sqcup \text{Disabled-}R)$$
  
(RDISAB3) Disabled will never become active anymore.  
 $\Sigma_{st} \models \text{Disabled-}R \sqsubseteq \Box^+ \neg R$   
(RDISAB4) Disabled classes can participate only in disabled  
relations.  
 $\Sigma_{st} \models \text{Disabled-}C_i \sqcap \Diamond^- \exists [U_i]R \sqsubseteq \exists [U_i]\text{Disabled-}R$ 

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## Constraints and logical implications

#### **PROPOSITION** (Status Relations: Logical Implications-cont'd)

- (RDISAB5) Disabled relations involve active, suspended, or disabled classes.
  - Disabled-R  $\sqsubseteq$  U<sub>i</sub>: (C<sub>i</sub>  $\sqcup$  Suspended-C<sub>i</sub>  $\sqcup$  Disabled-C<sub>i</sub>), for all i = 1, ..., n.

#### (RSCH3) Scheduled persists until active. $\Sigma_{st} \models \text{Scheduled-R} \sqsubseteq \text{Scheduled-R} \mathcal{U} \text{R}$

- (RSCH4) Scheduled cannot evolve directly to Disabled.  $\Sigma_{st} \models \text{Scheduled-R} \sqsubseteq \oplus \neg \text{Disabled-R}$
- (RSCH5) Scheduled relations do not involve disabled classes. Scheduled-R  $\sqsubseteq$  U<sub>i</sub>:¬Disabled-C<sub>i</sub>, for all i = 1, ..., n.

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# Life cycles





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## Mandatory & Exclusive

# $\begin{array}{ll} (\mathrm{ManP}) & \mathtt{W} \sqsubseteq \exists [\mathtt{whole}] \mathtt{PartWhole} \\ (\mathrm{ManW}) & \mathtt{P} \sqsubseteq \exists [\mathtt{part}] \mathtt{PartWhole} \\ (\mathrm{ExLP}) & \mathtt{P} \sqsubseteq \exists^{\leq 1} [\mathtt{part}] \mathtt{PartWhole} \\ (\mathrm{ExLW}) & \mathtt{W} \sqsubseteq \exists^{\leq 1} [\mathtt{whole}] \mathtt{PartWhole} \end{array}$

Mandatory Part Mandatory Whole Exclusive Part Exclusive Whole

Temporal ontologies

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Essential and immutable parts (details in [AGK08])

# Rigidity

## Definition (Rigid (+R))

A *rigid* property  $\phi$  is a property that is essential to *all* its instances, i.e.,  $\forall x \phi(x) \rightarrow \Box \phi(x)$ 

## Definition (Anti-Rigid ( $\sim$ R))

An *anti-rigid* property  $\phi$  is a property that is not essential to *all* its instances, i.e.,  $\forall x \phi(x) \rightarrow \neg \Box \phi(x)$ 

 $\begin{array}{ll} (\mathrm{Rigid}) & \texttt{C} \sqsubseteq \Box^*\texttt{C} \\ (\mathrm{A}\text{-}\mathrm{Rigid}) & \texttt{C} \sqsubseteq \diamondsuit^* \neg \texttt{C} \\ (\mathrm{A}\text{-}\mathrm{sub}\text{-}\mathrm{R}) & \texttt{C}_\texttt{A} \sqsubseteq \texttt{C}_\texttt{R} \end{array}$ 

Temporal ontologies

Modelling with temporal ontologies Summary

Essential and immutable parts (details in [AGK08])

#### Essential parts and wholes

- Essential parts are global properties of rigid wholes that can be formalized in DLR<sub>US</sub> with:
   (RIGIDW) W ⊑ □\*W Rigid Whole
   (EssP) W ⊑ ∃[whole]□\*PartWhole Essential Part
- Likewise for essential whole (RIGIDP) P ⊑ □\*P Rigid Part (EssW) P ⊏ ∃[part]□\*PartWhole Essential Whole

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Essential and immutable parts (details in [AGK08])

## Additional axioms for Immutable

(SUSW)	$\texttt{Suspended-PartWhole} \sqsubseteq \texttt{whole}: \texttt{Suspended-W}$
	Suspended Whole
(SUSP)	$\texttt{Suspended-PartWhole} \sqsubseteq \texttt{part}: \texttt{Suspended-P}$
	Suspended Part
(DISP)	Disabled-PartWhole 드 part : Disabled-P
	Disabled Part
(DISW)	$\texttt{Disabled} ext{-PartWhole} \sqsubseteq \texttt{whole} : \texttt{Disabled} ext{-W}$
	Disabled Whole
(SCHPW)	$ ext{PartWhole} \sqsubseteq \Diamond^-  ext{Scheduled-PartWhole}$
	Scheduled Part-Whole
(SCHP)	$\texttt{Scheduled-PartWhole} \sqsubseteq \texttt{part}: \texttt{Scheduled-P}$
	Scheduled Part
(SCHW)	$\texttt{Scheduled-PartWhole} \sqsubseteq \texttt{whole}: \texttt{Scheduled-W}$
	Scheduled Whole

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## Immutable part

#### Theorem (Immutable Parts)

Let  $W_R$  be a rigid class (i.e.,  $W_R \sqsubseteq \Box^* W_R$ ), W be an anti-rigid class (i.e.,  $W \sqsubseteq \Diamond^* \neg W$ ) s.t.  $W \sqsubseteq W_R$ , and PartWhole  $\sqsubseteq$  part :  $P \sqcap$  whole : W be a generic part-whole relation satisfying  $\Sigma_{st}$ . Then, for each whole,  $o_w$ , of type W there exists an immutable part,  $o_p$ , of type P that is temporally related to  $o_w$  with the relation:

- p2 holds if (MANP), (SUSW), (DISW) hold.
- p4 holds if (MANP), (SUSW), (DISW), (DISP) hold.
- p3 holds if (ManP), (SusW), (DisW), (SchPW), (SchP) hold.
- p1 holds if (ManP), (SusW), (DisW), (DisP), (SchPW), (SchP) hold.

Temporal ontologies

Essential and immutable parts (details in [AGK08])

## Immutable whole

#### Theorem (Immutable Wholes)

Let  $P_R$  be a rigid class (i.e.,  $P_R \sqsubseteq \Box^* P_R$ ), P be an anti-rigid class (i.e.,  $P \sqsubseteq \Diamond^* \neg P$ ) s.t.  $P \sqsubseteq P_R$ , and PartWhole  $\sqsubseteq$  part :  $P \sqcap$  whole : W be a generic part-whole relation satisfying  $\Sigma_{st}$ . Then, for each part,  $o_p$ , of type P there exists an immutable whole,  $o_w$ , of type W that is temporally related to  $o_p$  with the relation:

- w2 holds if (MANW), (SUSP), (DISP) hold.
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Essential and immutable parts (details in [AGK08])

# Life cycles





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# Life cycles



p4 holds if (MANP), (SUSW), (DISW), (DISP) hold.

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## The Boxer's hand (with p4)



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# The Boxer's hand (with p4)



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## The Boxer's hand (with p4)



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# Life cycles



p2 holds if (MANP), (SUSW), (DISW) hold.

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# Conclusions and current work

- Solution to the modeling problem of representing mandatory, immutable, and essential parts and wholes
- $\mathcal{ER}_{VT}$  augmented with *status relations* and its formalization into the temporal DL  $\mathcal{DLR}_{US}$

#### • Suspension

- TDL-Lite [AKL+07] (re temporal: with only  ${\cal U}$  and  $\oplus$  ; other variations recently investigated)
- Interaction with types of part-whole relations [KA08]
- Note: temporalizing relations is not unique to part-whole relations, but can be applied to any relation

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Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

## Motivation

- Preliminary categorizations and vocabularies of biological entities, focus on endurants
- With the maturing of (bio-)ontologies, scope is broadening to temporal aspects
- E.g., transformations, derivations, developments
  - the entity preserves its identity irrespective of the transformation while instantiating distinct classes at distinct points in time
- Questions arise:
  - What kind of entities are x and y instances of; phased sortals, roles, or merely different states?
  - How should one deal with the temporality to achieve implementable knowledge bases that can handle representations of, and reasoning over, transforming entities?

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Transforming objects (details in [Kee09])

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Mativation			

- Example definition for transformation\_of relation in the Relation Ontology [SCK+05]:
  "C transformation\_of C<sub>1</sub> = [definition] C and C<sub>1</sub> for all c, t, if Cct, then there is some t<sub>1</sub> such that C<sub>1</sub>ct<sub>1</sub>, and t<sub>1</sub> earlier t, and there is no t<sub>2</sub> such that Cct<sub>2</sub> and C<sub>1</sub>ct<sub>2</sub>."
- Two issues:
  - ignorant of the distinction between unidirectional transformations vs. where some instance of  $C_1$  may, after transforming into C, transform back into  $C_1$
  - does not say how the entities undergoing transformation are able to change and yet keep their identity;
- This under-specification can lead to unintended models of the theory

Temporal ontologies

Transforming objects (details in [Kee09])

# Preliminary definition

- Let *a* instantiate *C<sub>s</sub>* and *C<sub>t</sub>* at the two different times, with source and *t*arget the source is transformed into
- 'enough' properties are shared by a ∈ C<sub>s</sub> and a ∈ C<sub>t</sub> for identification as the same individual (a<sub>s</sub> =<sub>i</sub> a<sub>t</sub>)
- other properties π<sub>1</sub>...π<sub>n</sub> of a are lost or gained so that a instantiates a different universal after transformation

#### Definition ( $C_t$ transformation\_of $C_s$ )

Let  $C_t$  be the target and  $C_s$  the source universal, x, y range over instances and  $t_0, \ldots, t_n$  range over points in time, then  $C_t(x)$ *transformation\_of*  $C_s(y)$  iff for all x, there exist y,  $t_0, \ldots, t_n$ , if  $C_t(x, t_0)$ , then there is some  $t_1$  such that  $C_s(y, t_1)$ ,  $t_1 < t_0$ ,  $C_s$  and  $C_t$  have the same identity criterion ( $C_s =_i C_t$ ), x and y differ in at least one other property  $\pi_i$ , and there does not exist a  $t_2$  such that  $C_t(x, t_2)$  and  $C_s(y, t_2)$ .

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- other properties π<sub>1</sub>...π<sub>n</sub> of a are lost or gained so that a instantiates a different universal after transformation

#### Definition ( $C_t$ transformation\_of $C_s$ )

Let  $C_t$  be the target and  $C_s$  the source universal, x, y range over instances and  $t_0, \ldots, t_n$  range over points in time, then  $C_t(x)$ transformation\_of  $C_s(y)$  iff for all x, there exist y,  $t_0, \ldots, t_n$ , if  $C_t(x, t_0)$ , then there is some  $t_1$  such that  $C_s(y, t_1)$ ,  $t_1 < t_0$ ,  $C_s$  and  $C_t$  have the same identity criterion ( $C_s =_i C_t$ ), x and y differ in at least one other property  $\pi_i$ , and there does not exist a  $t_2$  such that  $C_t(x, t_2)$  and  $C_s(y, t_2)$ .

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

# OntoClean

- Uses the metaproperties of properties (unary predicates) to categorise types of entities [GW00a, GW00b]
- Rigidity, Identity, Unity, Dependence
- For instance, being a *Patient* and being a *Caterpillar* are ~R and being a *Person* and being a *Herbivore* are +R that may subsume *Patient* and *Caterpillar*

#### Definition (+R)

A *rigid* property  $\phi$  is a property that is essential to *all* its instances, i.e.,  $\forall x \phi(x) \rightarrow \Box \phi(x)$ 

#### Definition ( $\sim R$ )

An *anti-rigid* property  $\phi$  is a property that is not essential to *all* its instances, i.e.,  $\forall x \phi(x) \rightarrow \neg \Box \phi(x)$ 

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

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Temporal ontologies

Transforming objects (details in [Kee09])

# OntoClean

- *diachronic* identity (cf. synchronic identity)
- identity criteria (IC), which are both necessary and sufficient for identity
- +O property brings in its own identity criterion; properties that do not carry identity or do not supply identity are marked with -I and -O, respectively

#### Definition (+I)

A property that is not rigid carries an IC  $\Gamma$  iff it is subsumed by a rigid property carrying  $\Gamma.$ 

#### Definition (+0)

A property  $\phi$  supplies an IC  $\Gamma$  iff i) it is rigid; ii) it carries  $\Gamma$ ; and iii)  $\Gamma$  is not carried by all the properties subsuming  $\phi$ .

Introduction:	why	temporal	ontologies?

Transforming objects (details in [Kee09])

# OntoClean

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Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

#### Properties and their metaproperties

+0	+	+R	+D -D	Туре	
-0	+	+R	+D -D	Quasi-Type	Cartal
-0	+	~R	+D	Material role	Sortai
-0	+	~R	-D	Phased sortal	
-0	+	$\neg R$	+D -D	Mixin	
-0	-1	+R	+D -D	Category	
-0	-	~R	+D	Formal role	Non Sortal
		~R	-D		Non-Sonal
-0	-1	$\neg R$	+D -D	Attribution	

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

# Characterising the transforming entities

- (CT1) A phased sortal does not supply an IC, i.e., -O
- (CT2) A phased sortal must be subsumed by  $C_p$  that has +0
- (CT3) A phased sortal carries an IC, i.e., +I
- (CT4) A phased sortal is a sortal
- $(\mathrm{CT5})$  A phased sortal is anti-rigid, i.e.,  ${\sim}\mathsf{R}$

if  $C_t$  and  $C_s$  of the transformation\_of relation are both categorised as phased sortals, then:

(CT6)  $C_t$  and  $C_s$  both must be subsumed by  $C_p$ 

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

# Characterising the transforming entities

#### (CT7) $C_p$ must be a type (+O+I+R)

(CT8) Each type that subsumes phased sortals, which are related through the *transformation\_of* relation, must subsume *at least two* phased sortals

if  $C_t$  transformation\_of  $C_s$  and  $C_t$  and  $C_s$  are categorised as states, then the following constraints must hold:

(CT9)  $C_t$  and  $C_s$  must carry identity (+I)

(CT10) If  $C_t$  is a transformation of  $C_s$ , then it is possible, but not necessary, that at a later point in time  $C_t$ transforms back into  $C_s$ 

(CT11)  $C_t$  and  $C_s$  have meta-properties that are either  $\sim R$  or +R

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

## Characterising the transforming entities

- (CT12) If  $C_t$  and  $C_s$  are categorised as states, they are neither both types nor both roles
- (CT13) If  $C_t$  is a transformation of  $C_s$ ,  $C_t$  and  $C_s$  are phased sortals, then it is *not* possible that at a later point in time  $C_t$  is a transformation of  $C_s$ , i.e.,  $C_t$  does not transform back

Thus, based on foundational notions of Ontology, CT1-CT13 offers a more precise catergorisation for the relata of the *transformation\_of*, as well as their position in a taxonomy.
Temporal ontologies

Transforming objects (details in [Kee09])

## Temporal conceptual data modelling

- [APS07] have formalised the well-known core elements of temporal databases in  $\mathcal{DLR}_{\mathcal{US}}$  with corresponding  $\mathcal{ER}_{VT}$  that extends EER
- Does not take into account the kind of classes like phased sortal, but has *evolution constraints* and status classes
- *Status* is associated to a class to log the evolving status of membership of each object in the class and the relation between the statuses
  - E.g., when at t<sub>0</sub> object o ∈ Caterpillar (and o ∈
    Scheduled-Butterfly) starts transforming into an instance of
    Butterfly, then we have at the next time transformation at t<sub>1</sub>
    (with t<sub>0</sub> < t<sub>1</sub>) that o ∈ Disabled-Caterpillar and o ∈ Butterfly

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

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Introduction:	why	temporal	ontologies?

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

## Status classes



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Temporal ontologies

Transforming objects (details in [Kee09])

# Status property S

## Definition (+S)

A property  $\phi$  has status *active* at time *t* iff  $\phi(x)$  holds at time *t*.

## Definition (-S)

If a property  $\phi$  has status *scheduled* at time t then  $\phi(x)$  holds at some time  $t_0$ , for  $t_0 > t$ .

## Definition ( $\sim$ S)

If a property  $\phi$  has status *suspended* at time *t* then  $\phi(x)$  holds at some time  $t_0$ , with  $t_0 < t$ .

## Definition $(\neg S)$

A property  $\phi$  has status *disabled* at time t iff  $\phi$  holds at some time  $t_0$ , with  $t_0 < t$ , and for all t', such that  $t' \ge t$ ,  $\phi(x)$  does not hold.



When the instance *cannot* transform back:

- (CT14)  $C_s$  has +S at the time of transformation and  $\neg$ S after transformation
- (CT15)  $C_t$  has -S at the time of transformation and +S after transformation

If the entity *can* transform back, then CT14 and CT15 have to be replaced with:

- (CT14')  $C_s$  has +S at the time of transformation and either  $\neg$ S or  $\sim$ S after transformation
- (CT15')  $C_t$  has either -S or  $\sim$ S at the time of transformation and +S after transformation

Temporal ontologies

Modelling with temporal ontologies Summary

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Transforming objects (details in [Kee09])

# Status property S: position of classes in the taxonomy—transformation back possible

$$\phi^{+} \rightarrow \psi^{+} \quad (1)$$
  
$$\phi^{\sim} \rightarrow \psi^{\sim} \lor \psi^{+} \quad (2)$$
  
$$\phi^{\neg} \rightarrow \psi^{\neg} \lor \psi^{\sim} \lor \psi^{+} \quad (3)$$

 $\begin{array}{cc} \phi^{-} \rightarrow \neg \psi^{\neg} & (4) \\ \psi^{\neg} \wedge \diamond \phi^{+} \rightarrow \phi^{\neg} & (5) \end{array}$ 

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

# Status property S: position of classes in the taxonomy—no transformation back

$$\begin{array}{ccc} \phi^{+} \rightarrow \psi^{+} & (1) & \phi^{-} \rightarrow \neg \psi^{\neg} & (4) \\ & - & \psi^{\neg} \wedge \diamond \phi^{+} \rightarrow \phi^{\neg} & (5) \\ & - & \phi^{\neg} \rightarrow \psi^{\neg} \lor \psi^{+} & (6) \end{array}$$

- (1) & (4), CT6, CT14 & CT15 imply  $C_p^+$ , because always one of the phased sortals subsumed by  $C_p$  is active.
- Permitting suspension, ~S, then C<sup>+</sup><sub>p</sub> is also implied, because of (1), (2), (4), CT14' & CT15'

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

Status property S: position of classes in the taxonomy—no transformation back

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Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

## Reassessment of modelling choices

- Transformations like caterpillar and butterfly (phased sortals)
- Monocyte/macrophage transformation
  - Option 1: as phased sortals (known proposal); with CT14, CT15, but violating CT6, CT7, and CT8 (no suitable C<sub>p</sub>)
  - Option 2: as states (like in Physiome); CT1, CT3, CT5, CT9, CT10, CT11, CT12, CT14 & CT15
  - Option 3: somewhere in the taxonomy (FMA); cannot guarantee diachronic identity

### • Transforming healthy and pathological entities

- "Canonical" anatomy assumes healthy:  $C_p$ ?
- Non-curable diseases: CT9-CT12, CT14, CT15
- Curable diseases: CT9-CT12, CT14', CT15'

Temporal ontologies

Modelling with temporal ontologies Summary

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Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

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Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

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Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

# Recurring combinations

- i. Phased sortals, unidirectional transformation: CT1-CT8, CT13, CT14, CT15;
- ii. States (including quasi-types), unidirectional transformation: CT1-CT9, CT11-CT15;
- States (including quasi-types), transformation back is possible: CT1-CT13, CT14', CT15';
- iv. Pathological transformations, terminal disease: see constraints point ii, permit status change from -S directly into ¬S;
- v. Pathological transformations, reversal possible: see constraints point iii, permit status change from -S directly into  $\neg$ S.

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

## Conclusions and future directions

- Represent changing entities more precisely
- Kind of the participating entities and proposed, based on core ideas of the OntoClean approach
- Status property, generalised from temporal conceptual data modeling
- 17 constraints for transforming entities and its relation
- Assessment on applicability to bio-ontologies
- Implications of the interactions between OntoClean's property kinds, the status property, and temporal constraints in *DLR<sub>US</sub>* or the simpler TDL-Lite

Temporal ontologies

Modelling with temporal ontologies Summary

Transforming objects (details in [Kee09])

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Temporal ontologies

Modelling with temporal ontologies Summary

## Summary

- Introduction: why temporal ontologies?
  - Introduction
  - Temporal operators and relations
- 2 Temporal ontologies
  - Time ontology
  - DLR<sub>US</sub>
- Modelling with temporal ontologies
  - Essential and immutable parts (details in [AGK08])
  - Transforming objects (details in [Kee09])



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